

1 Does fixed-interval sampling suffice for water distribution system monitoring? An 2 adaptive strategy via time-frequency analysis

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4 **Abstract:** Sensors in water distribution systems (WDSs) generally use fixed-interval sampling, such as once
5 every 15 minutes, but whether this sampling frequency meets actual monitoring and modeling needs, has not
6 been sufficiently explored. This study continuously collected pressure monitoring data from three locations in a
7 WDS at a 100Hz sampling frequency for one month. Frequency analysis reveals that the signal is non-stationary,
8 with frequency characteristics varying significantly across different periods of the day. Since the information
9 content (e.g., high-frequency details) conveyed by the signal differs across time, this necessitates time-varying
10 sampling requirements to adequately capture critical data in each period. Based on these findings, an adaptive
11 sampling method (ASM) for WDS monitoring is proposed. Experimental results demonstrate that the proposed
12 ASM achieves a more uniform distribution of reconstruction error (i.e., the discrepancy between the original
13 high-frequency signal and its reconstruction from sampled data) and a lower overall error magnitude, compared
14 with the traditional fixed-interval sampling method (FISM). This study systematically investigates hydraulic data
15 sampling in WDSs under pressure conditions unaffected by anomalous variations, such as sudden pipe bursts or
16 extraordinary operational actions (e.g., valve maneuvers or atypical pump operations). The analysis is based on
17 signal characteristics and provides a foundation for the design of intelligent monitoring networks in WDSs.

18 **Keywords:** Adaptive Sampling, Fast Fourier Transform, Short-Time Fourier Transform, Water Distribution
19 System

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35 **Practical Applications:** This study updates the understanding of WDS hydraulic state dynamics, which
36 supports core water utility tasks such as online simulation and real-time scheduling, and confirms WDS hydraulic
37 states are dynamic, non-stationary processes rather than steady states that fixed-frequency sampling can fully
38 capture. Conventional fixed-frequency monitoring lacks systematic verification of its ability to capture WDS
39 dynamic changes, and has inherent flaws: it causes insufficient monitoring during high-variability periods, and
40 generates redundant data during low-variability periods, leading to unnecessary resource waste. The proposed
41 adaptive sampling method balances data accuracy and resource occupation; under the same sampling volume, it
42 achieves more uniform sampling error distribution, higher overall monitoring accuracy, and complete capture of
43 hydraulic changes that are easily overlooked by fixed-frequency sampling, providing a data-driven direction for
44 efficient WDS monitoring.

45

46 **Introduction**

47 In recent years, intelligent technologies have been increasingly applied in WDSs, encompassing hydraulic
48 models (Bartos et al. 2024), machine learning (Gross et al. 2025; Hao et al. 2022), and deep learning (Alvisi et
49 al. 2025; Hao et al. 2024). These technologies, serving as proactive management tools, focus on addressing core
50 issues in WDSs - such as state estimation (Rego et al. 2022), leakage detection (Daniel et al. 2022; Oberascher
51 et al. 2024), and district metering (Xie et al. 2024) - with their effective implementation relying crucially on
52 massive real-time monitoring data (Hu et al. 2023; Mahmoud et al. 2022; Zhang et al. 2023). Driven by this
53 growing reliance on continuous monitoring, pressure and flow sensors have become widely deployed in WDSs.
54 These sensors routinely transmit system measurements to the cloud at fixed intervals to support real-time
55 analytics and operational decision-making. However, despite the widespread adoption of 5 - 15-minute sampling
56 intervals in regions like the UK (Mounce et al. 2012) and China (Yu et al. 2022) for years, whether this fixed-
57 interval sampling suffices for WDS monitoring has not been fully explored.

58 While higher sensor sampling frequencies enhance data precision, practical engineering constraints
59 inherently limit their unrestricted increase. On the operational front, battery-powered sensors face proportional
60 increases in power consumption and data storage costs with higher sampling rates, straining water utilities'
61 maintenance budgets (Du et al. 2015). Technically, elevated sampling frequencies also overload hardware -
62 software systems by escalating data collection and processing demands (Cominola et al. 2018). This creates a
63 trade-off between balancing data precision and operational efficiency, a challenge that is central to intelligent
64 monitoring network design and operation.

65 Against this backdrop, while fields like agriculture (Zhang et al. 2024) , ecology (Lehtiniemi et al. 2022),
66 and hydrology (He et al. 2022) have systematically studied this relationship, WDSs remain underexplored.
67 Existing research on WDSs has primarily focused on water demand sampling (Cominola et al. 2018; Heydari et
68 al. 2022) and transient pressure sampling for burst detection (Mounce et al. 2012; Ye and Fenner 2014), as well
69 as determining minimum sampling frequencies for transient event detection (Kim et al. 2024b). In contrast,
70 pressure data in WDSs support a wide range of applications (Mounce et al. 2012; Ye and Fenner 2014), and the
71 networks typically operate under pressure conditions not affected by anomalous variations for the majority of the
72 time. The commonly adopted sampling interval of 5–15 minutes is based on assumptions corresponding to these
73 stable conditions. However, this practice has historically lacked comprehensive empirical validation from a signal
74 characteristics perspective.

75 The Nyquist - Shannon Sampling Theorem (Shannon 1949) dictates that reconstructing a continuous-time
76 signal from discrete samples without aliasing requires the sampling frequency to be at least twice the signal's
77 maximum frequency component-with a stricter standard recommending four times this value to capture wave
78 crests and troughs adequately (Choi et al. 2015). In the context of WDSs, this theorem presents unique challenges
79 because pressure signals exhibit pronounced dynamic characteristics driven by periodic variations as well as the
80 superimposed effects of operational and failure events. These dynamics mean that WDS signals can have
81 drastically different frequency profiles across days or even within the same day, as they are event related. Based
82 on the sampling theorem (Shannon 1949), sampling frequency should adapt: reduced when signals have low
83 frequencies to conserve power resources and increased during high-frequency events to maintain precision and
84 thus enhance event detection such as leaks and transient occasions. Yet existing fixed-interval sampling methods
85 (FISM; e.g., 5-minute intervals) overlook this temporal variability, failing to align with WDS signals' time-
86 varying nature, thus instantly requiring the development of adaptive sensor sampling algorithms to meet changing
87 monitoring requirements.

88 Adaptive sensor sampling strategies, by optimizing the number of sampling points across different time
89 periods (i.e., sampling intervals), offer a promising solution to balance data precision and operational efficiency
90 without increasing overall data volume. While such strategies have been applied in domains like agriculture
91 (Rodriguez-Pabon et al. 2022) and greenhouse monitoring - where Kochhar et al. (2023) adjusted frequencies by
92 comparing temporal data trends. However, WDS sensor signals differ fundamentally in two key aspects. First,
93 they are driven by regular daily cycles in water demand, resulting in periodic fluctuations that are not commonly
94 addressed in previous ASM studies (Hu et al. 2021; Huang et al. 2021; Ristow et al. 2021). Second, they are
95 subjected to abrupt, high-impact disturbances (e.g., pump startups, pipe bursts, environmental noise), introducing
96 non-stationary frequency components that far exceed the variability seen in, for instance, greenhouse humidity
97 or soil moisture signals (Song et al. 2023; Wu et al. 2024; Zhang et al. 2024). This dual nature - periodic yet
98 influenced by various operational disturbances and failure events - makes WDS signals unique. Unlike adaptive
99 algorithms designed for environmental data, existing methods fail to account for WDS signals' time-varying
100 frequency profiles and abrupt transient events. As the dynamic frequency characteristics of WDS remain
101 understudied, there is an urgent need to develop adaptive sampling frameworks that explicitly adapt to both the
102 daily periodicity and operational disturbances and failure events, ensuring optimal data quality while minimizing
103 operational costs.

104 To address this gap in understanding how to optimize sampling frequency for WDS pressure data,
105 particularly from the perspective of the signal's inherent time-varying characteristics, this study collected high-
106 frequency pressure data from an operational WDS in a southern Chinese city. To address this unmet need, this
107 study first characterized the signal's non-stationary frequency dynamics using Fast Fourier Transform (FFT) and
108 Short-Time Fourier Transform (STFT) time-frequency analyses, revealing distinct daily periodicity and abrupt
109 frequency shifts driven by real-world disturbances. These insights formed the basis for developing a stable ASM
110 that adjusts intervals according to instantaneous frequency content. Analysis results show that, under the same
111 data volume condition, the proposed strategy not only achieves higher data precision but also ensures a more
112 uniform distribution of reconstruction errors, effectively balancing data quality and operational efficiency in
113 WDS monitoring. This work represents a new systematic exploration of hydraulic data sampling in WDS from a
114 signal-characteristics perspective, providing a foundation for intelligent monitoring networks in WDS.

115 **2. Materials and Methodology**

116 **2.1 Data Collection**

117 The high-frequency monitoring data used in this study were obtained from a large-scale, real-world WDS
118 in China. The system is equipped with three pressure sensors, which are installed at different locations within the
119 network: a main pipeline, a terminal node, and a regional pump station. The sensor sampling frequency was set
120 to 100 Hz, which is the highest frequency used in previous studies (Choi et al. 2015; Kim et al. 2024a; b) to
121 ensure the collected data closely capture actual pressure behavior, while maintaining a balance between data
122 volume and accuracy. The monitoring data were collected over a 30-day period. Data for the terminal node
123 spanned 22 days, owing to temporary equipment maintenance during the monitoring period. The sensor
124 installation locations are shown in Figure 1, where the main pipeline is highlighted in red. Additionally, Figure
125 2 illustrates the pressure time series recorded over a 1-week period at the three sampling sites, complementing
126 the spatial-temporal data presented in Figure 1.

127 **2.2 Frequency Analysis of Pressure Data**

128 To analyze the overall frequency distribution of the monitoring data, frequency-domain analysis was
129 performed on the pressure data from the three sampling sites using the FFT. Additionally, the STFT was applied
130 to analyze the periodic variations in the pressure signal frequencies and how they change at different times.

131 **2.2.1 Fast Fourier Transform (FFT)**

132 The Fourier Transform is a widely used signal processing tool that converts time-domain signals into their
133 frequency-domain representations, thereby revealing the spectral characteristics of the signal. However, the
134 traditional Discrete Fourier Transform has a high computational complexity of $O(N^2)$, which makes it
135 impractical for large-scale data analysis. To overcome this, the FFT algorithm, which reduces the computational
136 complexity to $O(N \log N)$, was employed in this study, significantly improving computational efficiency.

137 In this work, FFT was applied to perform frequency-domain analysis on the collected pressure data to
138 identify the primary frequency components. Given a discrete signal $\mathbf{x}(n)$ of length N , the FFT is defined as:

$$139 \quad \mathbf{m}(f) = FFT(p_1, p_2, \dots, p_N) \quad (1)$$

140 where, $\mathbf{m}(f)$ represents the energy associated with different frequency f ; $FFT(\cdot)$ denotes the Fast Fourier
141 Transform; and p_1, p_2, \dots, p_N refer to the pressure data used in the transformation, with N being the total number
142 of pressure data points.

143 FFT enables efficient global spectral analysis of the pressure signal, ignoring temporal frequency
144 variations to enhance computational efficiency and frequency resolution. By transforming the pressure signal
145 from the time domain to the frequency domain, FFT reveals the constituent frequency components and their
146 energy distribution, thereby providing a theoretical basis for determining an appropriate sampling frequency for
147 pressure monitoring in WDSs.

148 **2.2.2 Short-Time Fourier Transform (STFT)**

149 While FFT is effective at revealing the overall frequency distribution of a signal, it assumes that the signal
150 is stationary over the entire time domain (i.e., its statistical properties do not change over time). However, real-
151 world signals are often non-stationary, with their spectral characteristics varying over time. To address this, the
152 STFT was applied for time-frequency analysis.

153 The STFT segments the signal using a sliding window function, such that each segment can be treated as
154 stationary. FFT is then applied to each windowed segment to obtain spectral information that varies over time.
155 The STFT is defined as:

$$156 \quad \mathbf{m}(f, t) = STFT(p_1, p_2, \dots, p_N) \quad (2)$$

157 where, $\mathbf{m}(f, t)$ represents the signal energy at frequency f within the time window centered at t ; $STFT(\cdot)$
 158 denotes the Short-Time Fourier Transform. After applying the transformation, the energy distribution across
 159 different frequencies can be obtained for each time window. In this study, a Hanning window was specifically
 160 employed to reduce spectral leakage. Optimized window length and overlap ratio were chosen using the grid
 161 search algorithm to achieve better time and frequency resolution. The computed time-frequency spectrograms
 162 were used to analyze the signal's frequency characteristics across time, illuminating its dynamic properties.

163 As a valuable complement to the FFT, the STFT divides the original pressure signal into multiple short
 164 time windows and performs an FFT on each segment, thereby capturing the time-varying frequency content of
 165 the signal. By capturing time-varying frequency features, this process provides a scientific basis for developing
 166 more effective and rational sampling strategies, thereby bridging the gap between signal characteristics and
 167 adaptive sampling design. This method enables the identification of non-stationary characteristics in pressure
 168 data, making it particularly suitable for analyzing dynamic behaviors in WDSs.

169 **2.3 Adaptive Sampling Strategy Design**

170 ***2.3.1 Adaptive Sampling interval optimization***

171 In current engineering practice, the most commonly used FISM assumes that the signal remains stationary
 172 throughout the data collection process. However, in practical applications, the pressure monitoring data exhibit
 173 significant non-stationarity, with the energy distribution of frequency components varying over time. Based on
 174 the STFT analysis, an ASM was proposed, in which the sampling frequency is dynamically adjusted according
 175 to the energy of the frequency components in different time periods. This approach enhances the ability to capture
 176 critical variations in the pressure signal while improving the efficiency and accuracy of data acquisition.

177 After obtaining the energy distribution across time and frequency using Eq. (2), the energy of the pressure
 178 signal is first normalized along the frequency dimension.

$$179 \quad \hat{\mathbf{m}}(f, t) = \frac{\mathbf{m}(f, t) - \min_t\{\mathbf{m}(f, t)\}}{\max_t\{\mathbf{m}(f, t)\} - \min_t\{\mathbf{m}(f, t)\}} \quad (3)$$

180 where, $\hat{\mathbf{m}}(f, t)$ represents the normalized energy distribution of different frequency f within the time window
 181 centered at t ; $\max_t\{\mathbf{m}(f, t)\}$ and $\min_t\{\mathbf{m}(f, t)\}$ are the maximum and minimum energy for all time window.

182 At each time window, for mitigating the influence of high-frequency noise in the pressure signal, a low-
 183 pass filter is applied to remove the spectral energy components above the cutoff frequency:

184
$$\ddot{\mathbf{m}}(f, t) = \widehat{\mathbf{m}}(f, t), f \leq f_c \quad (4)$$

185 where, f_c is the cutoff frequency, and $\ddot{\mathbf{m}}(f, t)$ represents the truncated energy distribution.

186 Furthermore, the mean of the truncated energy distribution along the frequency dimension is first
187 calculated.

188
$$\bar{\mathbf{m}}(t) = \frac{\sum_{f=0}^{f_c} \ddot{\mathbf{m}}(f, t)}{n} \quad (5)$$

189 where, $\bar{\mathbf{m}}(t)$ is the mean of the truncated energy distribution along the frequency dimension, and n is the total
190 number of frequency components.

191 Then, for each time window, the variance of the energy distribution across different frequency
192 components can be calculated as follows:

193
$$var(t) = \frac{\sum_{f=0}^{f_c} [\ddot{\mathbf{m}}(f, t) - \bar{\mathbf{m}}(f, t)]^2}{n - 1} \quad (6)$$

194 where, $var(t)$ is the variance of the energy distribution across different frequency components.

195 By using $var(t)$ as the weighting factor for sample allocation, the number of samples assigned to each
196 time window can be calculated:

197
$$s_t = M \frac{[var(t)]^\gamma}{\sum_{t=0}^T [var(t)]^\gamma} \quad (7)$$

198 where, s_t is the number of samples allocated to the time window centered at t ; M is the predefined total number
199 of samples per day; and γ is the exponent parameter of the variance, used to adjust the importance of the variance
200 in the allocation process.

201 The proposed sampling strategy consists of three main components. The first component involves
202 performing time-frequency analysis on daily pressure data using the STFT. The second component calculates the
203 variance of the energy for each sliding window. The third component assigns different numbers of sampling
204 points to each window based on the variance of the energy. The rationale behind this proposed strategy is that
205 the pressure in WDSs primarily occupies lower-frequency regions. When the sliding window moves into periods
206 dominated by low-frequency signals, the variance in energy is small, leading to fewer sampling points, which are
207 sufficient for capturing the low-frequency signals. Conversely, when the window encompasses periods with both

208 low - and high-frequency signal distributions, the variance in energy increases, resulting in more sampling points
209 to adequately capture the higher-frequency signals.

210 **2.3.2 Moving Average Sampling**

211 To mitigate the inevitable noise impact on single-sample data, a Moving Average Sampling (MAS)
212 strategy is adopted. This approach involves collecting m consecutive samples at a fixed interval (e.g., 0.01s
213 between each sample) and computing their mean as the representative value for that sampling period:

$$214 \quad \check{y}_i = \sum_{j=i-k}^{i+k} y_j \quad (8)$$

215 where, \check{y}_i is the sampled value at time step i , and the parameter $2k + 1$, representing the number of consecutive
216 samples, which is optimized to balance noise reduction and data efficiency. By leveraging the statistical property
217 that random noise tends to cancel out in averaged values, MAS effectively attenuates high-frequency disturbances
218 while preserving the underlying signal trend. By adjusting m based on real-time noise levels or signal
219 characteristics (e.g., using grid search or adaptive algorithms), the strategy can dynamically optimize the trade-
220 off between noise suppression and sampling overhead, making it suitable for diverse monitoring scenarios in
221 WDSs or other sensor networks.

222 **2.4 Sampling Simulation and Evaluation**

223 In the sampling evaluation, the data for both FISM and ASM were generated by subsampling the high-
224 frequency (100 Hz) pressure data. If the sampled values were compared with the original high-frequency data
225 only at the sampling instants (i.e., direct sampling), the resulting error would always be zero, which fails to reflect
226 the actual performance of the algorithms. Therefore, to robustly evaluate the proposed ASM, an assessment
227 method was developed to overcome the limitation of direct sampling. The approach involves:

- 228 1) Sampling data from the original 100 Hz signal using the algorithm to simulate real-world sensor sampling.
- 229 2) Reconstructing 100 Hz data via interpolation between sampling points, as direct sampling alone cannot
230 evaluate accuracy.
- 231 3) Applying a moving average filter (MAF) to the original noisy data, then using residual magnitude and
232 distribution uniformity between reconstructed and filtered data as evaluation metrics.

233 The mean absolute error (MAE) between the reconstructed and filtered data as evaluation metrics. The
234 MAE is calculated as:

$$MAE = \frac{1}{N} \sum_{i=1}^N |y_i - \hat{y}_i| \quad (9)$$

where N is the number of samples, y_i is the true value of the i -th sample, and \hat{y}_i is the predicted value for the i -th sample. The absolute difference $|y_i - \hat{y}_i|$ represents the error between the true and predicted values for each sample.

Beyond absolute error, the temporal uniformity of reconstruction errors is selected as another metric. This is achieved by computing the standard deviation of the MAE for each hour using the following formulation:

$$STD = \sqrt{\frac{\sum_{i=1}^N \{|y_i - \hat{y}_i| - MAE\}^2}{N - 1}} \quad (10)$$

3. Results and Analysis

3.1 Frequency Content Analysis

3.1.1 Frequency Domain Analysis

Figure 2 shows the pressure time series recorded at the three monitoring sites. Overall, the pressures at all sites fluctuate within a relatively stable range. The mean pressures at Sensor #1, Sensor #2, and Sensor #3 are approximately 29.9 m, 30.3 m, and 41 m, respectively, each displaying clear periodic variations. The diurnal patterns at Sensors #1 and #2 are mainly driven by daily water-demand cycles, whereas the periodicity at Site #3 is associated with scheduled pump operations. All three datasets also exhibit random fluctuations and occasional outliers, indicating the presence of measurement noise—a well-recognized issue in pressure data acquisition (Mounce et al. 2012; Shao et al. 2024; Zhao et al. 2017).

FFT was applied to examine the pressure data in the frequency domain. Figure 3 shows the FFT results for the three sampling sites. The signal energy is mainly concentrated in the low-frequency band, whereas the high-frequency components contain only minor energy. This indicates that pressure dynamics are dominated by low-frequency variations, consistent with the fact that pressure changes in WDSs are largely driven by daily water-demand cycles.

According to Choi et al. (2015), the sampling frequency should be at least four times the highest significant frequency component to ensure accurate signal representation. Accordingly, Figure 3 marks the maximum frequency detectable under a 10-minute sampling interval using red dashed lines. The spectral results

260 show that most high-energy components of the pressure signal lie within this detectable range, suggesting that
261 the commonly used 10-minute interval is generally sufficient for characterizing steady-state behavior in WDSs.
262 However, this assessment assumes that the pressure signal is fully stationary. From an average perspective, the
263 10-minute interval appears appropriate, but the inherent non-stationarity of pressure data implies that the actual
264 required sampling frequency may be considerably higher. Therefore, in practice, the sampling rate should be
265 adaptively adjusted to account for the signal's non-stationary characteristics, ensuring a more accurate reflection
266 of system dynamics.

267 ***3.1.2 Time-Frequency Domain Analysis***

268 To further examine the time–frequency characteristics of the pressure data, the STFT was applied to the
269 measurements from the three sampling sites. The window length plays a critical role in shaping the time–
270 frequency representation: longer windows provide better frequency resolution but smooth short-term variations,
271 whereas shorter windows improve temporal resolution while diminishing the ability to distinguish low-frequency
272 components. Given that pressure signals in WDSs are dominated by low-frequency dynamics, excessively short
273 windows may obscure these dominant features, while overly long windows may suppress meaningful high-
274 frequency fluctuations.

275 To balance these trade-offs and capture frequency dynamics across multiple temporal scales, three
276 window lengths were selected. The 2-day window enables analysis of inter-day frequency variations, the 2-hour
277 window provides a balanced resolution suitable for characterizing intra-day dynamics, and the 20-minute window
278 offers finer temporal detail while preserving sufficient low-frequency resolution. Together, these windows
279 support a comprehensive assessment of the time-varying frequency characteristics of the pressure signals.

280 Figures 4a–4c present the STFT results for the three sampling sites using a 2-day window with a 1-day
281 overlap. As the sliding window progresses along the time axis, the energy distribution across frequencies varies,
282 demonstrating that the pressure data are not stationary. The dominant frequency components at all three sites
283 remain concentrated in the low-frequency range, consistent with the FFT results.

284 Figures 4d–4f show the STFT results for the three sampling sites using a 2-hour window with a 1-hour
285 overlap. For each site, the STFT was first applied to the daily pressure data, and the resulting energy values were
286 then averaged. The results indicate that all three sites exhibit pronounced high-frequency components during
287 specific periods of the day, while low-frequency components dominate the remaining periods. At the terminal
288 and main-pipe sites, notable high-frequency activity occurs between 5:00–8:00 am, 4:00–5:00 pm, and 11:00–

289 12:00 pm. At the pump station, high-frequency components are most prominent from 6:00–11:00 am. These
290 temporal patterns show that the pressure signals undergo significant fluctuations at certain times of the day but
291 remain relatively stable during others, highlighting the non-stationary nature of the data—contrary to the
292 stationarity assumed in the FFT analysis.

293 Similar to Figures 4d–4f, Figures 4g–4i present the STFT results for the three sampling sites using a 20-
294 minute window with a 10-minute overlap. Comparing Figures 4g–4i with Figures 4d–4f shows that longer
295 windows capture more low-frequency components, whereas shorter windows highlight higher-frequency
296 variations. Thus, the choice of window length substantially influences the STFT results. Nevertheless, this
297 variation does not change the main conclusion: the pressure data in the WDS are inherently non-stationary,
298 exhibiting pronounced high-frequency components during certain periods and predominantly low-frequency
299 components during others.

300 The time–frequency analysis shows that periods with elevated high-frequency energy correspond to a
301 greater need for higher sampling frequencies. For the terminal and main pipeline sites, stronger high-frequency
302 components occur between 5:00–8:00, 16:00–17:00, and 23:00–24:00. At the pump station, this occurs between
303 6:00–11:00. In contrast, during periods with lower high-frequency energy, the required sampling frequency is
304 correspondingly reduced.

305 To quantify the sampling requirements over time, the variance of spectral energy within each time window
306 was used as an indicator. Higher variance indicates stronger high-frequency fluctuations and thus a greater
307 sampling demand, while lower variance reflects energy concentrated in the low-frequency range and a reduced
308 sampling need. Figure 5 presents the spectral energy variance across 2-hour windows with 50% overlap for
309 Sensor #1, Sensor #2, and Sensor #3, using cutoff frequencies of 0.28, 0.6, and 0.88, respectively. With the 50%
310 overlap, the effective time resolution is 1 hour.

311 As illustrated by the comparison of Figures 4 and 5, the spectral energy variance effectively captures
312 temporal variations in sampling requirements. In Figure 5(a), the variance is notably high between 5:00 and 8:00
313 each day, indicating the need for increased sampling frequency during this period. Consistently, Figure 4(d)
314 shows a more dispersed energy distribution over the same interval, demonstrating that the variance-based metric
315 reliably reflects the non-stationary behavior of pressure data in the WDS. Building on this insight, an ASM is
316 proposed, where the number of samples allocated to each period is determined according to the quantified demand
317 derived from spectral energy variance.

318 **3.2 Adaptive Sampling**

319 Previous studies have generally assumed that pressure sensors in WDSs follow a FISM, implicitly
320 presuming that system pressure remains completely stable over time (Chu et al. 2021; Santos-Fernandez et al.
321 2024; Zhou et al. 2023). However, the analysis in the previous section demonstrates that this assumption is invalid.
322 Consequently, applying a uniform sampling frequency throughout the day leads to under-sampling during periods
323 with high-frequency activity and over-sampling when low-frequency components dominate, resulting in uneven
324 information capture. This unevenness is evident in the reconstruction errors when low-frequency sampled data
325 are used to reconstruct the underlying true signal, showing variable error distributions across the day. To address
326 this issue, an ASM was developed based on the variance of spectral energy within sliding time–frequency
327 windows. Windows with higher variance are assigned more sampling points, whereas those with lower variance
328 receive fewer samples (Eq. (7)).

329 **3.2.1 High-frequency Data Denoising**

330 In this study, a MAF was applied to the high-frequency (100 Hz) pressure data to remove noise and
331 estimate the underlying true signal. This filtered signal was used as the reference baseline for assessing the
332 performance of different sampling strategies. The MAF window length was optimized through a systematic trial-
333 and-error process over a range of 20, 40, 60, 80, 100, and 120 s, with a final value of 1 min selected to balance
334 effective high-frequency noise reduction and the preservation of meaningful signal dynamics.

335 Figure 6 compares the raw and denoised pressure signals recorded over three consecutive days at the three
336 sampling sites. The denoised signals exhibit smoother profiles, more accurately reflecting the true variations in
337 system pressure. In contrast, the high-frequency fluctuations around the filtered signal in the raw data represent
338 stochastic disturbances within the system, which are effectively removed by the denoising process.

339 **3.2.2 Accuracy of Reconstruction Data**

340 In the proposed ASM, the parameter γ in Eq. (7) controls the influence of spectral energy variance on
341 sample allocation. Larger γ values increase the weight of variance, whereas smaller values reduce it. Based on a
342 systematic evaluation of $\gamma = 1, 2,$ and 3 using the objective function STD defined in Eq. (10), the optimal γ was
343 determined to be 1 for Sensor #1 and Sensor #2, and 2 for Sensor #3. In addition, the window length significantly
344 affects the time–frequency energy distribution, which in turn shapes the variance across time periods: longer
345 windows emphasize low-frequency components, while shorter windows highlight high-frequency variations. To
346 reduce the influence of high-frequency noise, frequencies above the designated cutoff were excluded when

347 computing variance, ensuring that the variance distribution more accurately reflects the actual situation. Optimal
348 window lengths and cutoff frequencies under different sampling conditions were determined using a grid
349 optimization algorithm, with the objective function STD defined in Eq. (10). The resulting optimized parameters
350 are summarized in Tables S1 and S2, which are provided in the Supporting Information.

351 Figure 7b presents the reconstruction error histograms for each hourly period when 288 samples are
352 collected (i.e., FISM interval of 5 minutes) at Sensor #1, comparing the FISM strategy with the proposed ASM.
353 The ASM markedly reduces overall reconstruction errors compared to FISM, with the MAE decreasing from
354 0.1128 to 0.0746. This improvement stems from the ASM's ability to optimize the sampling distribution by
355 allocating points according to the varying demands of different periods. For example, during the 7th hourly time
356 window, the pressure signal contains more high-frequency components, and FISM produces large errors. In
357 contrast, the 21st hourly time window is dominated by low-frequency components, resulting in smaller errors
358 under FISM. The ASM addresses this by assigning more samples to high-demand periods like the 7th hourly
359 time window and fewer to low-demand periods like the 21st hourly time window, thereby improving overall
360 sampling efficiency. Reconstruction errors under different sites and sampling quantities are summarized in Table
361 1 and Figures S1–S21, with the latter provided in the Supporting Information, which are consistent with this
362 analysis.

363 Figures 7a and 7c show the reconstruction error histograms for each hourly period when 960 and 48
364 samples are collected (i.e., FISM intervals of 1.5 minutes and 30 minutes) at Sensor #1, comparing the FISM
365 approach with the proposed ASM. As before, applying the ASM substantially reduces reconstruction errors.
366 However, the improvement becomes less pronounced at lower sampling rates. This is because reduced sampling
367 increases interpolation errors, which limits the relative information gain achieved through optimized sample
368 allocation.

369 ***3.2.3 Error Uniformity of Reconstruction Data***

370 Regarding error uniformity, Figure 7b shows that the ASM markedly improves the uniformity of pressure
371 reconstruction errors at all three sampling sites compared to the FISM approach. For Sensor #1, the uniformity
372 metric STD decreased from 0.0344 under FISM to 0.0149 with ASM. This improvement arises from the ASM's
373 refined allocation of sample points: windows with stronger high-frequency components are assigned more
374 samples, while those with weaker high-frequency content receive fewer samples. Reconstruction error uniformity
375 across different sites and sampling quantities is summarized in Table 1 and Figures S1–S21 in the Supporting

376 Information. These results align with the preceding analysis, further demonstrating the robustness and
377 generalizability of the proposed ASM.

378 As shown in Figures 7a and 7c, the ASM improves the uniformity of pressure reconstruction errors across
379 different sample quantities. When 960 samples are used, the uniformity metric *STD* decreases from 0.0248 under
380 FISM to 0.0059 with ASM. For 48 samples, *STD* decreases from 0.0533 to 0.0401. Figure 7 demonstrates similar
381 trends across different sampling quantities. However, as the number of samples decreases, the improvement in
382 uniformity becomes less pronounced. This is primarily because fewer samples limit the number of points that
383 can be allocated to each window, reducing the refinement of the adaptive sampling process. As a result, subtle
384 variations in the pressure signal's frequency are harder to capture, leading to smaller performance gains with
385 ASM. However, this limitation is reasonable, as achieving highly refined sample allocation with very few
386 samples is inherently challenging.

387 **Discussion**

388 This study addressed the critical question of whether FISM suffices for WDS pressure monitoring, and
389 proposed ASM grounded in time-frequency analysis. The core outcome— that ASM outperforms FISM in
390 reducing overall reconstruction error and improving error uniformity— stems from its ability to align sampling
391 frequency with the non-stationary nature of WDS pressure signals. Unlike FISM, which assumes signal
392 stationarity and leads to under-sampling during high-variability periods and over-sampling in low-variability
393 phases, ASM dynamically allocates sampling points based on spectral energy variance (Eq.(6)), ensuring critical
394 high-frequency details are captured without redundant data. This alignment with the Nyquist-Shannon Sampling
395 Theorem addresses the long-standing trade-off between data precision and operational efficiency in WDS
396 monitoring, providing a data-driven solution for intelligent sensor network design.

397 Beyond the primary performance gains, the study's time-frequency analysis (FFT and STFT) offers
398 deeper insights into WDS hydraulic dynamics: pressure signals are dominated by low-frequency components
399 driven by daily water demand cycles, yet exhibit pronounced high-frequency fluctuations during specific time
400 windows (e.g., 5:00–8:00 am). This finding challenges the implicit assumption of steady-state pressure in
401 conventional monitoring, emphasizing that sampling strategies must account for temporal variability to avoid
402 information loss. However, the proposed ASM has inherent methodological limitations: using spectral energy
403 variance as the sampling allocation metric may occasionally misreflect high-frequency component proportions—
404 significant variance can arise even in predominantly low-frequency signals, potentially wasting sampling

405 resources. While setting a cutoff frequency to partition high- and low-frequency bands is a conceptual solution,
406 noise-induced spectral distortion complicates optimal cutoff determination, limiting generalizability.
407 Additionally, the reliance on basic FFT and STFT, while practical for implementation, may insufficiently capture
408 extreme non-stationarity or transient events; advanced techniques like wavelet analysis or semblance analysis
409 could enhance resolution for complex WDS environments.

410 The findings are derived from 30-day high-frequency data (22 days for one sensor) collected from three
411 locations in a single WDS, and spectral characteristics of pressure signals may vary across different WDS types,
412 geographical settings, or seasons. While the observed sampling demand trends are generalizable, ASM
413 parameters (e.g., window length, γ) must be tailored to specific deployment contexts. Practically, this requires
414 short-term high-frequency pre-sampling (e.g., 100 Hz) to characterize site-specific signal dynamics, a step that
415 ensures adaptability but adds initial setup overhead.

416 Although the ASM demonstrates clear advantages, its applicability may not be universal in certain
417 scenarios. For example, ASM may not be suitable for water balance analysis. In water distribution network
418 districts with multiple inlets and outlets, applying ASM to flow data could result in temporally misaligned signals,
419 thereby hindering accurate estimation of net inflow. Similarly, the analysis of pressure fluctuations induced by
420 demand variations requires temporal alignment between pressure and flow-rate signals. The development of more
421 flexible adaptive sampling strategies to accommodate diverse data application scenarios will be explored in future
422 work.

423 **Conclusions**

424 For a long time, FISM has been used in WDSs sensor sampling. To assess whether this fixed interval is
425 sufficient to capture the essential monitoring information and to better reflect the distribution of information
426 within the data, this study investigates the required sampling frequency for pressure monitoring in WDSs and
427 proposes an ASM. The objective is to identify a more appropriate sampling frequency and strategy for WDS
428 monitoring in order to more accurately enhance the effectiveness of information acquisition and ensure the
429 reliable operation of water infrastructure. Based on the analysis and the proposed ASM, the following key
430 findings and practical implications are summarized:

- 431 (1) Through frequency domain analysis using the FFT, it was found that the widely adopted 10-minute sampling
432 interval captures most pressure data information on average based on the assumption that the pressure signal
433 behaves as a stationary time series.
- 434 (2) In practice, the pressure signal in WDSs is non-stationary. STFT analysis reveals that the pressure signal
435 exhibits varying frequency characteristics across different periods of the day, resulting in time-varying
436 sampling requirements. Certain periods exhibit higher energy in the high-frequency components, indicating
437 a greater need for dense sampling, whereas other periods have lower sampling demands.
- 438 (3) Considering the non-stationary nature of pressure signals, this study proposed an ASM that accounts for the
439 time-varying sampling demand by quantifying the energy variance of different frequency components
440 derived from the STFT. The results show that, compared with the traditional FISM, the proposed strategy
441 achieves more uniform sampling error distribution and lower overall error magnitude.

442 The limitations of the present study are that the above findings are based on high-frequency pressure data
443 collected from three sensors in a single WDS, and the applicability and specific parameters of the ASM require
444 tailored settings based on specific scenarios. Future research should address these limitations by: 1) validating
445 the ASM across diverse WDSs (e.g., urban vs. rural, small vs. large-scale) and seasonal conditions to optimize
446 parameter adaptability; 2) integrating advanced time-frequency analysis techniques to refine the sampling
447 allocation metric, balancing accuracy and operational feasibility; 3) exploring the integration of the ASM with
448 real-time noise reduction algorithms to mitigate the impacts of spectral distortion. 4) developing more flexible
449 adaptive sampling strategies to accommodate a wide range of complex data application scenarios. By addressing
450 these gaps, the adaptive sampling framework can be further refined to support more robust and cost-effective
451 WDS monitoring, advancing the development of intelligent water infrastructure management systems.

452 **Data availability Statement**

453 Data will be made available on request.

454 **Acknowledgments**

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458 **Conflict of Interest**

459 The authors declare that they have no known competing financial interests or personal relationships that
460 could have appeared to influence the work reported in this paper.

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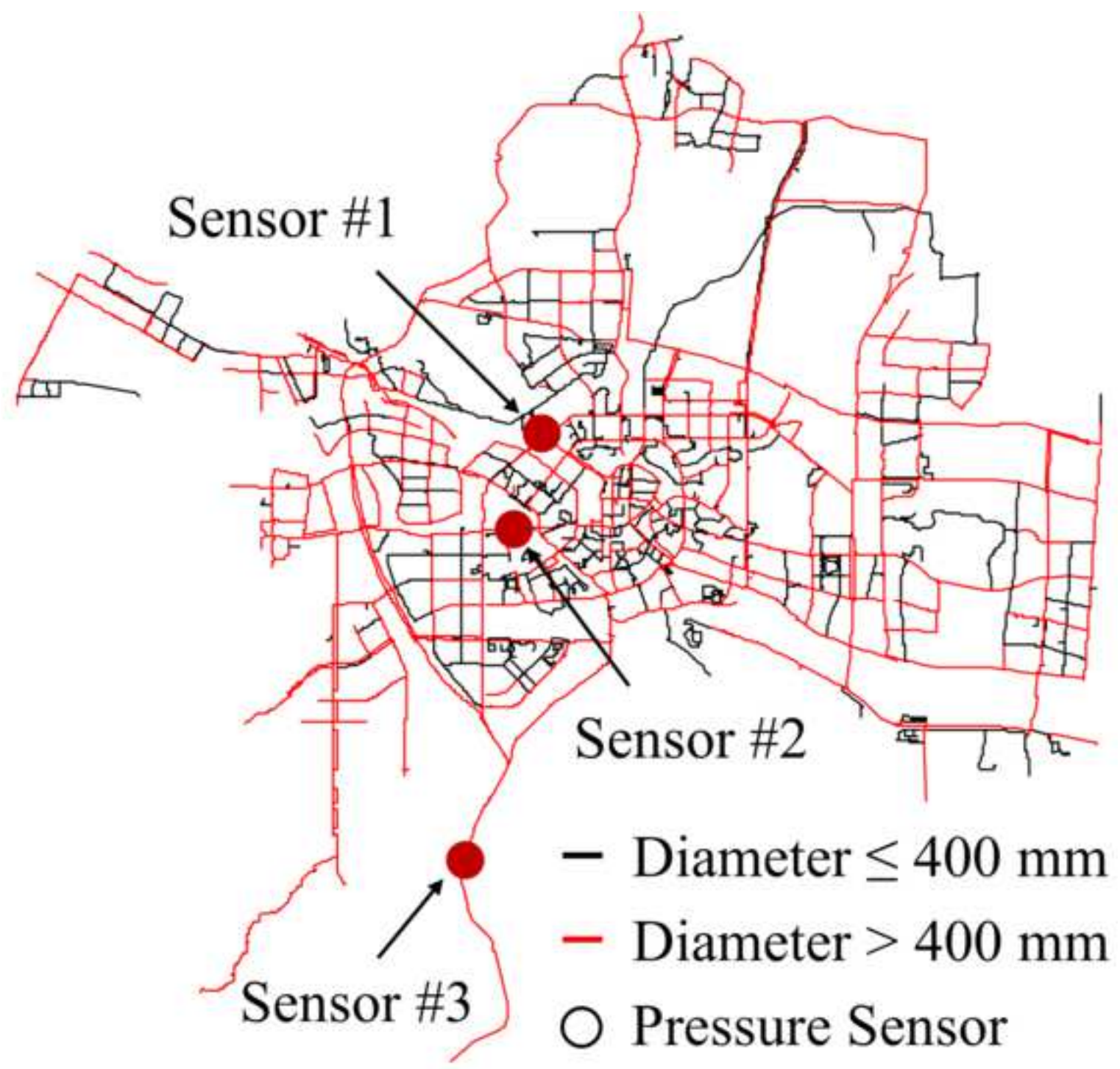
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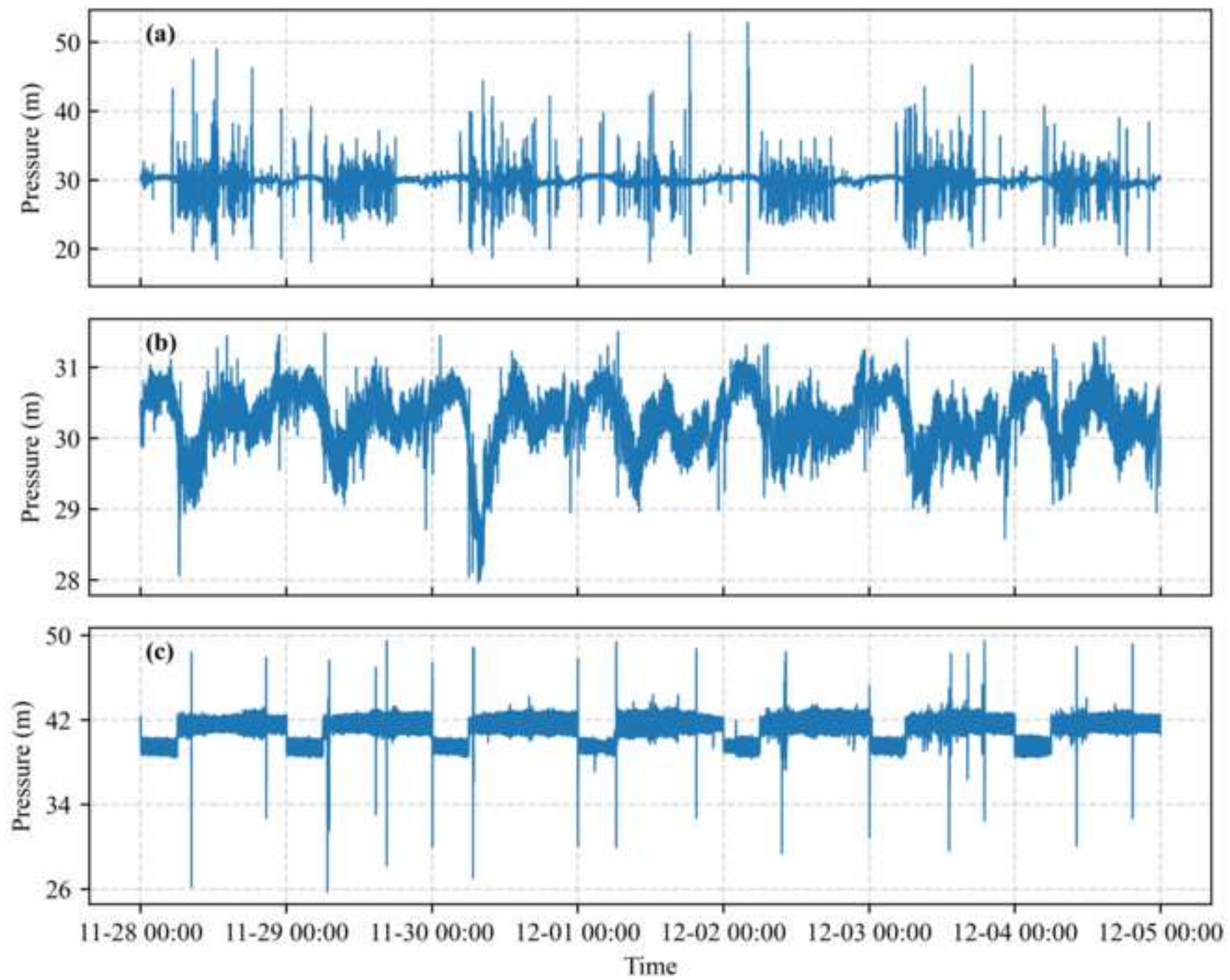
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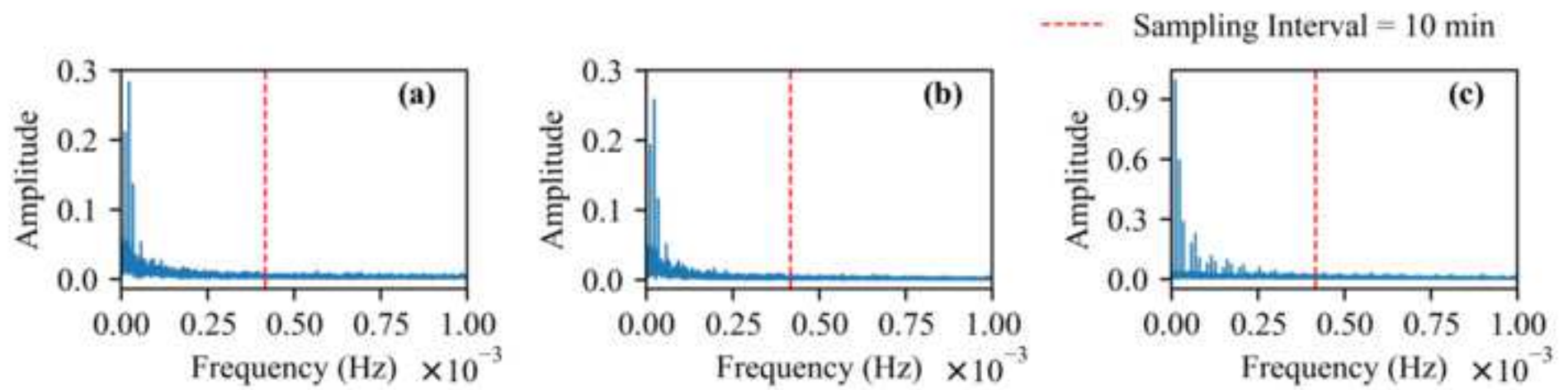
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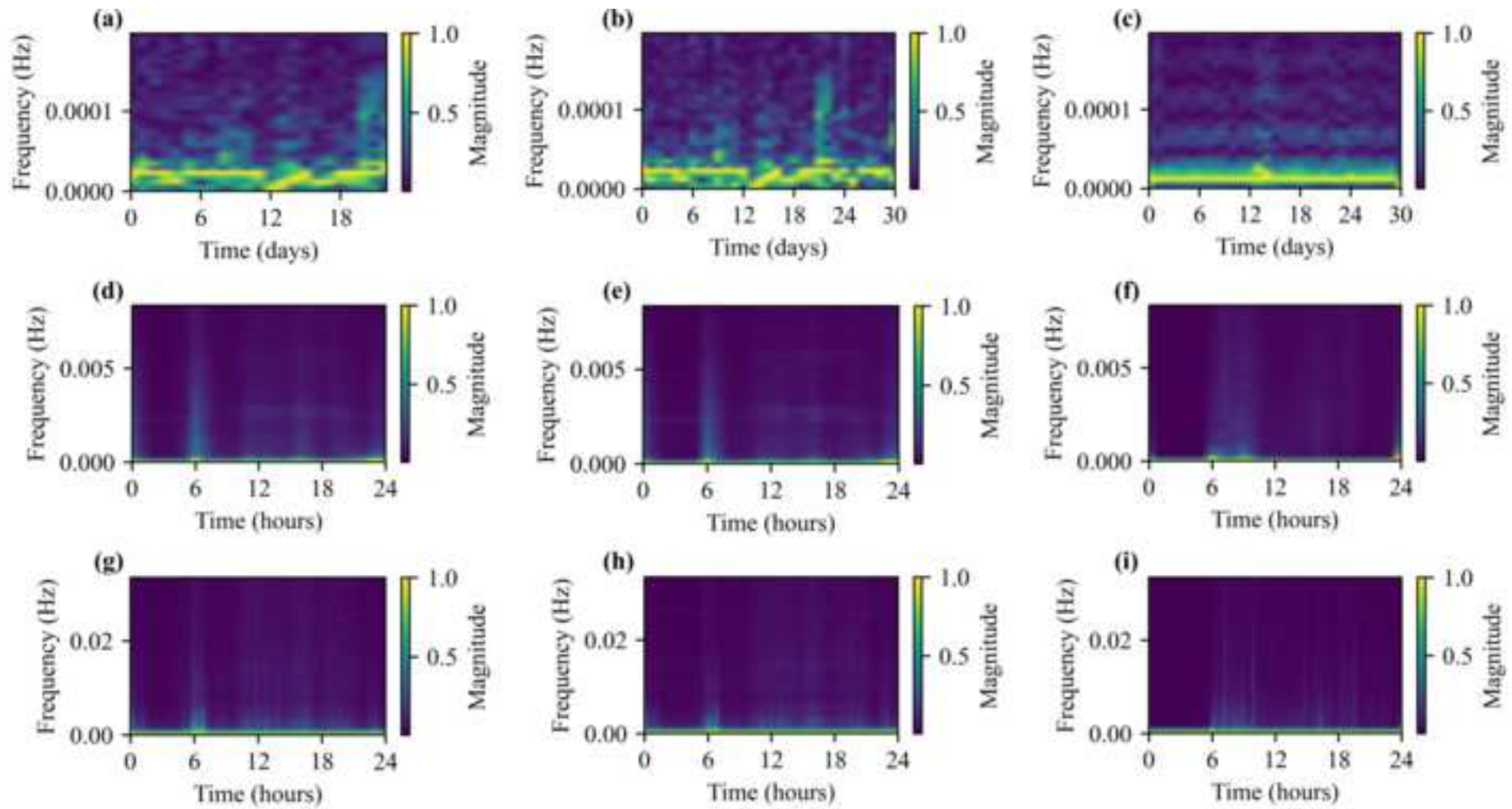
Table 1. Reconstruction error metrics of FISM and ASM under different sampling quantities for three sensors.

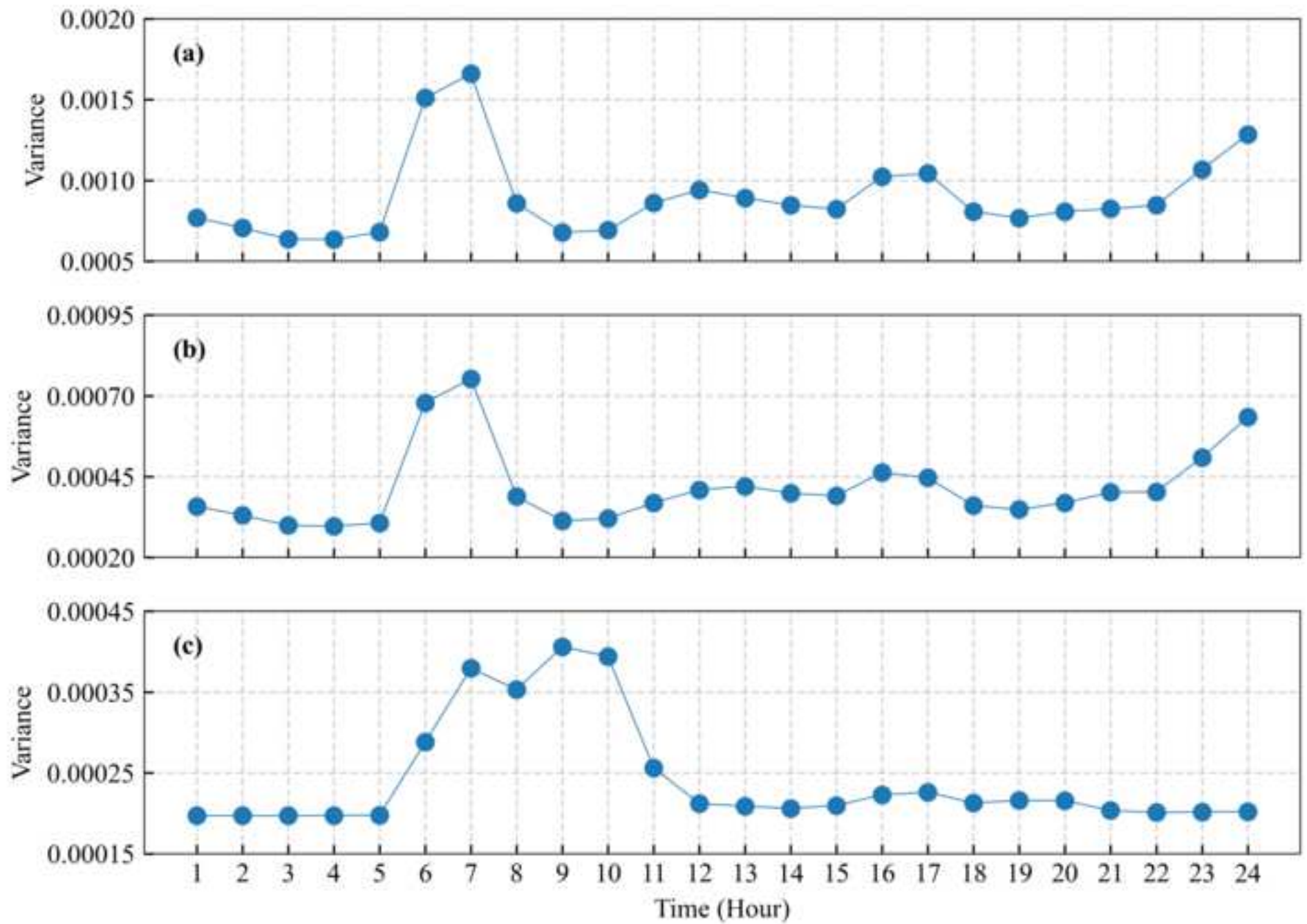
Sensor	Metric	Method	Sampling quantities							
			960	480	288	192	144	96	72	48
Sensor #1	MAE	FISM	0.083	0.095	0.113	0.123	0.129	0.138	0.141	0.153
		ASM	0.029	0.053	0.075	0.086	0.097	0.108	0.114	0.125
	STD	FISM	0.025	0.028	0.034	0.038	0.046	0.047	0.049	0.053
		ASM	0.006	0.011	0.015	0.022	0.028	0.029	0.034	0.040
Sensor #2	MAE	FISM	0.062	0.074	0.088	0.097	0.100	0.110	0.115	0.124
		ASM	0.025	0.047	0.066	0.075	0.083	0.093	0.098	0.109
	STD	FISM	0.013	0.016	0.021	0.026	0.029	0.034	0.039	0.044
		ASM	0.004	0.008	0.012	0.015	0.021	0.024	0.028	0.033
Sensor #3	MAE	FISM	0.170	0.187	0.206	0.218	0.222	0.239	0.244	0.267
		ASM	0.038	0.072	0.097	0.114	0.128	0.145	0.154	0.169
	STD	FISM	0.033	0.044	0.054	0.063	0.068	0.079	0.087	0.103
		ASM	0.014	0.029	0.040	0.050	0.057	0.069	0.076	0.095

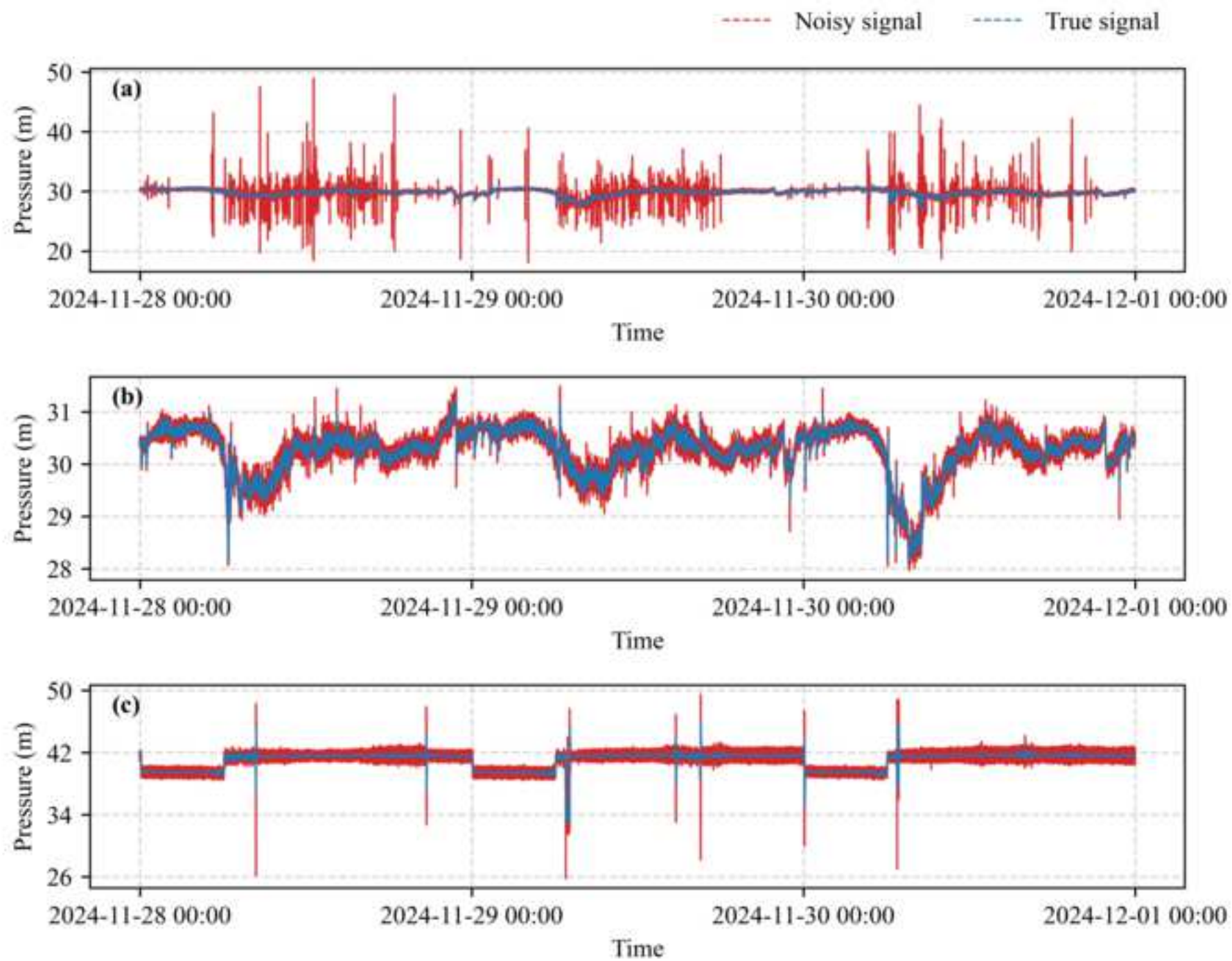












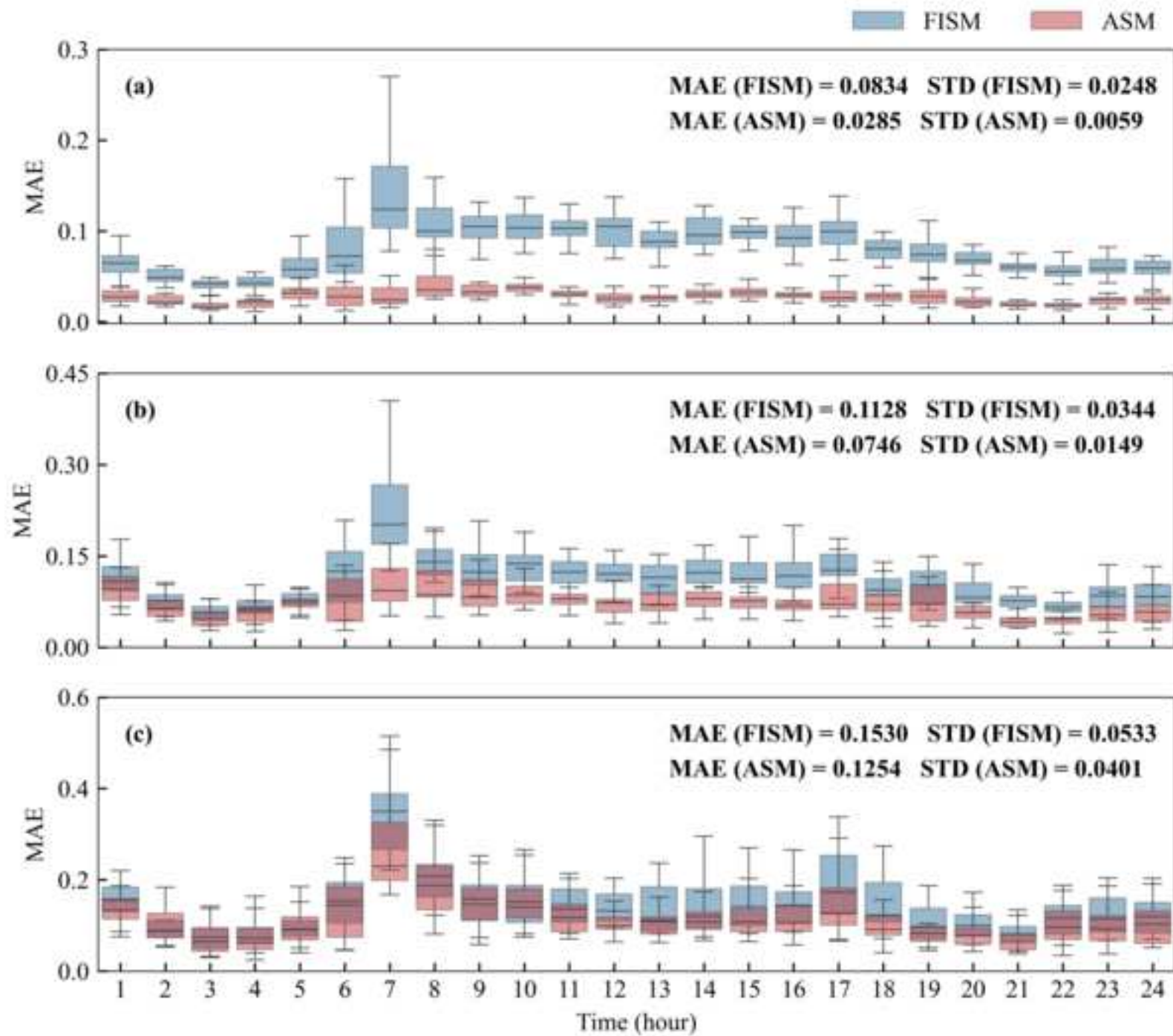


Fig. 1. Sensor installation locations, with red pipes denoting pipelines larger than 400 mm in diameter.

Fig. 2. Pressure time series for a 1-week period recorded at three sampling sites: (a) Sensor #1; (b) Sensor #2; (c) Sensor #3.

Fig. 3. FFT analysis results of pressure data recorded at three sampling sites: (a) Sensor #1; (b) Sensor #2; (c) Sensor #3.

Fig. 4. Time–frequency spectrograms of three sampling sites under different window lengths: (a) Sensor #1, 2 days; (b) Sensor #2, 2 days; (c) Sensor #3, 2 days; (d) Sensor #1, 2 hours; (e) Sensor #2, 2 hours; (f) Sensor #3, 2 hours; (g) Sensor #1, 20 minutes; (h) Sensor #2, 20 minutes; (i) Sensor #3, 20 minutes.

Fig. 5. Distribution of spectral energy variance across different time windows: (a) Sensor #1; (b) Sensor #2; (c) Sensor #3.

Fig. 6. Noisy signals and estimated true signals at the three sampling sites: (a) Sensor #1; (b) Sensor #2; (c) Sensor #3.

Fig. 7. Comparison of reconstruction error distributions after applying FISM and ASM at Sensor #1: (a) 960 samples; (b) 288 samples; (c) 48 samples.